CAMBRIDGE INTERNATIONAL EXAMINATIONS

International General Certificate of Secondary Education

MARK SCHEME for the May/June 2014 series

0580 MATHEMATICS

0580/43 Paper 4 (Extended), maximum raw mark 130

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Abbreviations

cao correct answer only

dep dependent

FT follow through after error isw ignore subsequent working

oe or equivalent SC Special Case

nfww not from wrong working

soi seen or implied

Qu		Answers	Mark	Part Marks
1	(a)	62100[.00] Final answer	2	B1 for 62 074[. 35] or 62 070
	(b)	39300	3	M2 for 45 981÷ 1.17 oe or M1 for 45 981 associated with 117 [%]
	(c)	20436	2	M1 for $45981 \div (3+4+2)$ or 45981×4
	(d)	4	3	M2 for $\frac{1.5 \times 1000}{330}$ oe
				or M1 for figs 4545 or 455
	(e)	25545	2	M1 for $45981 \times \frac{5}{9}$
2	(a)	$ 10 < x \le 25 25 < x \le 30 30 < x \le 35 35 < x \le 50 50 < x \le 60 $	2	5 correct B1 for 3 or 4 correct or SC1 for all correct but in the form 10 to 25 or 10 – 25
		13 33 19 [4] 15 6	3	B2 for 4 correct or B1 for 3 correct
	(b)	25.1[0] or 25.13 to 25.14 nfww	4	M1 for mid-values soi, condone one error or omission 5 17.5 27.5 32.5 42.5 55 soi and M1 for $\sum fx$ for any x in intervals including boundaries, but all f s must be integers, condone one further error or omission
				and M1 dep for $\sum fx \div 90$
				Dep on 2nd M mark earned

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Qu		Answers	Mark	Part Marks
3	(a) (i)	72[.0] or 71.98 to 71.99 nfww	3	M2 for [sin P =] $\frac{97}{\frac{1}{2} \times 12 \times 17}$ oe or M1 for implicit version
	(ii)	16.2 or 16.18 to 16.19 nfww	4	M2 for $6^2 + 17^2 - 2 \times 6 \times 17 \times \cos(their 72)$ or M1 for implicit form
				and A1 for $[XR^2 =] 261.8$ to 262
	(b)	7.61 or 7.612 nfww	4	M3 for $[a =] 9.4 \times \sin 37 \div \cos 42$ oe or $[a =] 9.4 \sin 37/\sin(90-42)$
				or M2 for [$a =$] their height ÷ cos 42 oe or $\frac{a}{\sin 37} = \frac{9.4}{\sin(90 - 42)}$ oe
				or M1 for their height $\div a = \cos 42$ or for [their height =] $9.4 \times \sin 37$ oe
				or B1 for 48° correctly used or seen in correct position on diagram
	(c)	50	1	
		130	1	
4	(a)	0, 4.5, 3.11[1]	3	B1, B1, B1
	(b)	Complete correct curve with	5	B3 FT for 9 points correctly plotted
		minimum below $y = 2$		B2 FT for 7 or 8 points correctly plotted
		1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1		and B1 indep two separate branches not touching or cutting <i>y</i> -axis
	(c)	- 0.5 to - 0.6	1	
		0.6 to 0.7 2.8 to 2.9	1 1	if 0 SC1 for $y = 3$ indicated
	(d)	Correct line or no line and - 0.7 to - 0.6 nfww	3	Must check line - not if wrong line B2 for $y = 1 - x$ ruled correctly
				or SC1 for ruled line with either gradient –1 or <i>y</i> -intercept 1 but not line y = 1 or correct freehand line

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Qu			Answers	Mark	Part Marks
	(e)		tangent ruled at $x = 2$ and 0.62 to 0.8	3	Accept integer/integer provided in range B1 for correct tangent drawn
					and M1 for change in y / change in x dep on any tangent or close attempt at tangent at any point Must see correct or implied calculation from a drawn tangent
	(f)		$\frac{1}{x^2} = -x \text{ or } 1 + x^3 = 0$	M1	
			$1 = -x^3 \text{ or } x^3 = -1$	M1	dep M1
			$x = \sqrt[3]{-1}$	A1	dep M2
5	(a)	(i)	$\begin{pmatrix} 2 \\ 4 \end{pmatrix}$	1	
		(ii)	5.83 to 5.831	2	M1 for $3^2 + 5^2$ seen
	(b)	(i)	$-2\mathbf{p} + \mathbf{q}$ oe	1	accept unsimplified
		(ii)	$\overrightarrow{PS} = -\mathbf{p} + 2\mathbf{q} \text{ or } \overrightarrow{SP} = \mathbf{p} - 2\mathbf{q}$	B1	
			$\overline{MS} = -\frac{2}{3}\mathbf{p} + \frac{4}{3}\mathbf{q}$ seen	B1	
			or $\overrightarrow{SM} = \frac{2}{3} \mathbf{p} - \frac{4}{3} \mathbf{q}$ seen		
			or $\overrightarrow{RM} = \frac{2}{3} (-2\mathbf{p} + \mathbf{q})$ soi		
			or $\overrightarrow{MR} = \frac{2}{3} (2\mathbf{p} - \mathbf{q}) \text{ soi}$		
			or $\overline{MQ} = \frac{1}{3}(-2\mathbf{p} + \mathbf{q})$ soi		
			or $\overline{QM} = \frac{1}{3}(2\mathbf{p} - \mathbf{q})$ soi		
			$\overrightarrow{PM} = \mathbf{p} + \overrightarrow{RM}$	M1	Any correct route for \overrightarrow{PM} eg $\overrightarrow{PR} + \overrightarrow{RM}$
			or $\mathbf{p} - \overline{MR}$		
			$\left[= -\frac{1}{3} \mathbf{p} + \frac{2}{3} \mathbf{q} \right]$		
			1 : 3 nfww	A1	After 0 scored, SC1 for 1:3

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Qu			Answers	Mark	Part Marks
6	(a)	(i)	$\frac{1}{6}$	1	
		(ii)	$\frac{4}{6}$ oe	1	
		(iii)	$\frac{2}{6}$ oe	1	
	(b)		$\frac{16}{36}$ oe	3	M2 $\frac{2}{6} \times \frac{4}{6} + \frac{4}{6} \times \frac{2}{6}$ only oe
					or M1 for one of $\frac{2}{6} \times \frac{4}{6}$ or $\frac{4}{6} \times \frac{2}{6}$ soi by $\frac{2}{9}$
	(c)		$\frac{48}{360}$ oe	3	M2 for $\frac{4}{6} \times \frac{3}{5} \times \frac{2}{4} \times \frac{2}{3}$ only oe or M1 for denominators 6, 5, 4, 3 soi in product of four fractions
7	(a)	(i)	148	1	
		(ii)	122	2	B1 for 58 seen at <i>A</i> or 32 seen at <i>Y</i>
		(iii)	148	1	
		(iv)	106 nfww	3	B1 for [sum of interior angles =] 720
					and M1 for $\frac{1}{2} \{ (their 720) - (p+q+t+90) \}$
	(b)	(i)	63	2	B1 for angle $RPS = 27$ or 90 at P or at S seen or stated
		(ii)	54	2	B1 for <i>their x</i> or 63 or letter <i>x</i> at <i>Q</i> seen or state

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Qu		Answers	Mark	Part Marks
8	(a) (i)	$7 \times 2 + (2x - 3)(x + 4) = 2(x + 4)$	M1	Allow if bracket[s] omitted but recovers
		$2x^2 + 8x - 3x - 12$ or better seen	B1	
		$2x^2 + 3x - 6 = 0$	A1	with no errors seen and brackets correctly expanded on both sides and no omission of brackets
	(ii)	$\sqrt{(3)^2 - 4(2(-6))}$ or better $p = -3$ and $r = 2(2)$	B1	or $\left(x + \frac{3}{4}\right)^2$
			B1	Must see $\frac{p+\sqrt{q}}{r}$ or $\frac{p-\sqrt{q}}{r}$ or both
				Or $-\frac{3}{4} + \text{or} - \sqrt{\frac{57}{16}}$
		1.14 and – 2.64 cao	B1B1	SC1 for 1.1 and – 2.6 final answer or 1.137 and – 2.637 final answer or 1.14 and – 2.64 seen in working or for -1.14 and 2.64 as final ans
	(b)	$\pi \times x^2 + \pi \times x \times 3x$	M2	or M1 for $\pi \times x \times 3x$
		$4[\pi]x^2 = [\pi]r^2$	M1	Dep on M2
		2x = r	A1	with no errors seen
9	(a)	4 - 6x final answer	1	
	(b)	9x - 8 final answer	2	M1 for $4 - 3(4 - 3x)$ seen
	(c)	$\frac{1}{27}$ final answer	3	M2 for 3^{-3} soi by final answer 0.037037 to 3sf or better or M1 for $[g(-1)=]$ 3 soi
	(d)	$\frac{4-x}{3}$ oe final answer	2	M1 for a correct first step $3x = 4 - y \text{ oe or } x = 4 - 3y \text{ or } \frac{y}{3} = \frac{4}{3} - x$
	(e)	$\frac{4}{3}$ or $1\frac{1}{3}$ or 1.33 or better	3	M2 for $3x - 4 = 0$ or better
				or M1 for $3^{-(4-3x)}$

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Qu		Answers	Mark	Part Marks
10	(a)	[r=] 2.30[9]	3	B2 for [r =] 2.31
				or M2 for 4 tan 30
				or M1 for $\frac{r}{4} = \tan 30$
	(b)	333 or 332.5 to 332.6	4	M3 for $0.5 \times 8 \times 8 \times \sin 60 \times 12$ oe or M2 for $0.5 \times 8 \times 8 \times \sin 60$ oe or M1 for <i>their</i> triangle area \times 12 shown
				dep on ' $\frac{1}{2}$ ' used within <i>their</i> area of triangle method
	(c) (i)	30	3	M2 for 12 ÷ 0.4 or 120 ÷ 4 or SC1 for figs 3
	(ii)	6.65 or 6.647 to 6.648[]	2	M1 for $\pi \times 2.3^2 \times 0.4$
				or SC1 for $\pi \times 2.3^2 \times 4$ soi by 66.5 or 66.47 to 66.48[]
	(iii)	40[.0] or 40.1 or 40.0 to 40.2 nfww	3	M2 for $100 - \frac{their(c)(i) \times their(c)(ii)}{their(b)} \times 100$
				or $\frac{their(b) - their(c)(i) \times their(c)(ii)}{their(b)} \times 100$
				or M1 for $\frac{their(c)(i) \times their(c)(ii)}{their(b)} \times 100$
				or $\frac{their(b) - their(c)(i) \times their(c)(ii)}{their(b)}$
11	(a)	$\frac{1}{8} \frac{1}{16} \frac{1}{32}$	2	B1 for 2 correct
		$\frac{1}{2^{n-1}}$ oe	2	SC1 for $\frac{1}{2^n}$ oe
		$2^{-3} 2^{-4} 2^{-5}$	1	
		2^{1-n} or $2^{-(n-1)}$	1	
	(b) (i)	64 256 1024	1	
		$2^6 \ 2^8 \ 2^{10}$	1	
	(ii)	$2^{2(n-1)}$ or 2^{2n-2}	1	
	(c)	16384	2	B1 for $n = 8$